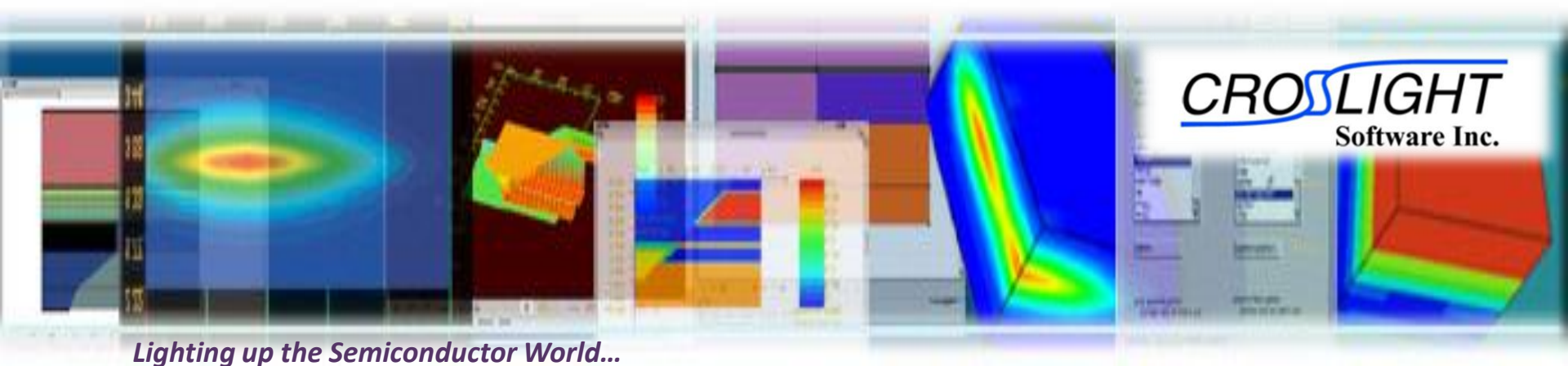


Simulation of Quantum Cascade Lasers

© 2005-2010 Crosslight Software Inc.






Lighting up the Semiconductor World...

Contents

- 👉 **Microscopic rate equation approach**
- 👉 Challenge in carrier transport modeling
- 👉 Solution in 2/3D simulator

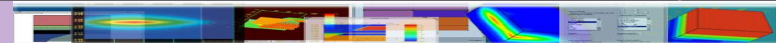
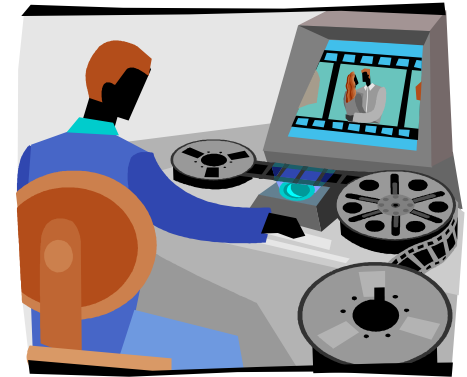
Subband engineering

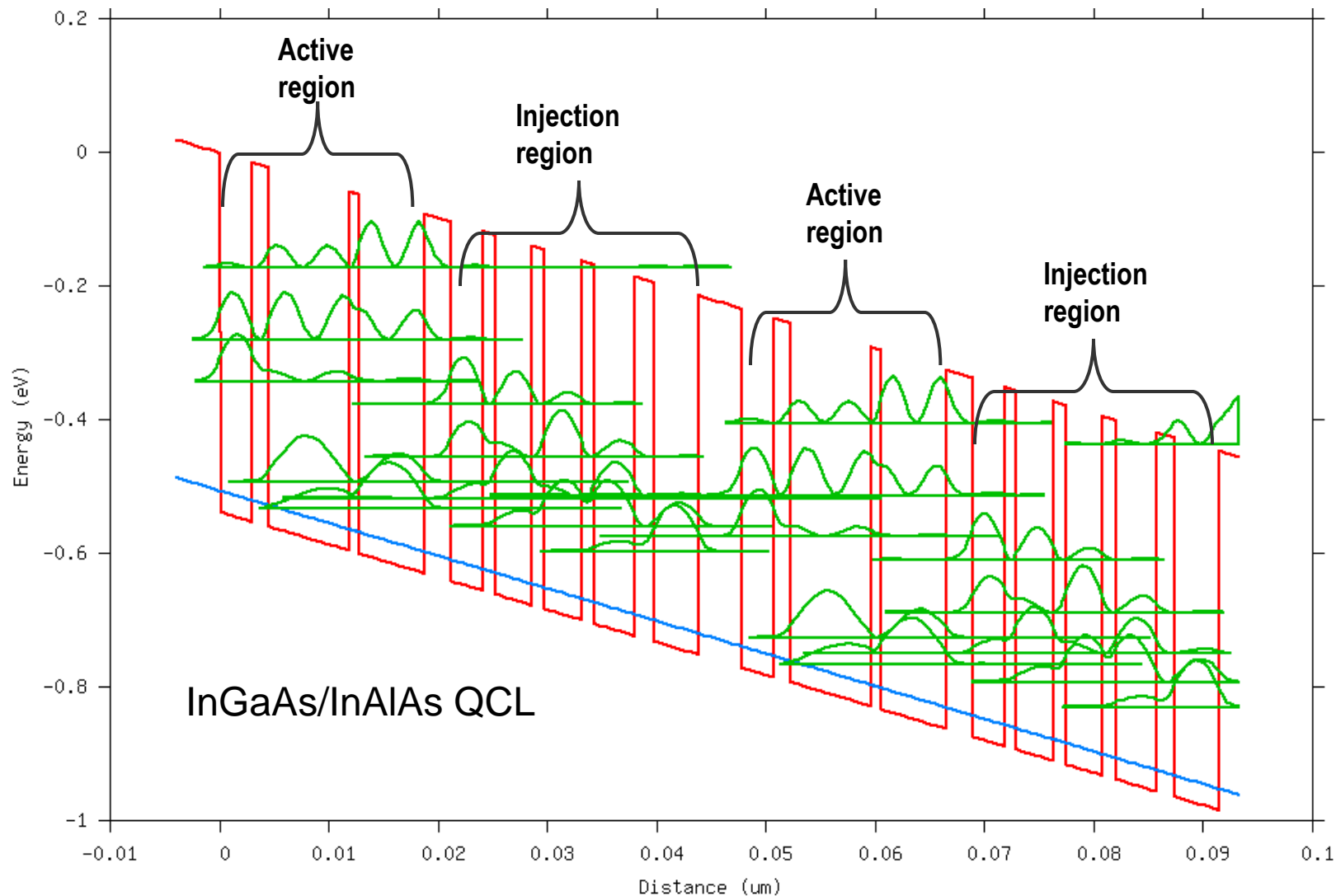
-  Given MQW structure, all quantum states are solved.
-  Energy levels and intersubband transition dipole moments computed for all pairs of states.
-  Critical states identified according to design ideas such as the so-called 3-level design.



Simulation procedures

- 📊 Set up 1D mesh for two periods of QCL in gain-preview session.
- 📊 Assume a uniform applied field and solve the quantum states.
- 📊 Discretize Schrodinger equation in 1D and solve with sparse eigen matrix techniques.
- 📊 Identify and label states belonging to injection or active regions, based on shape and location of wave functions and their respective energy levels.

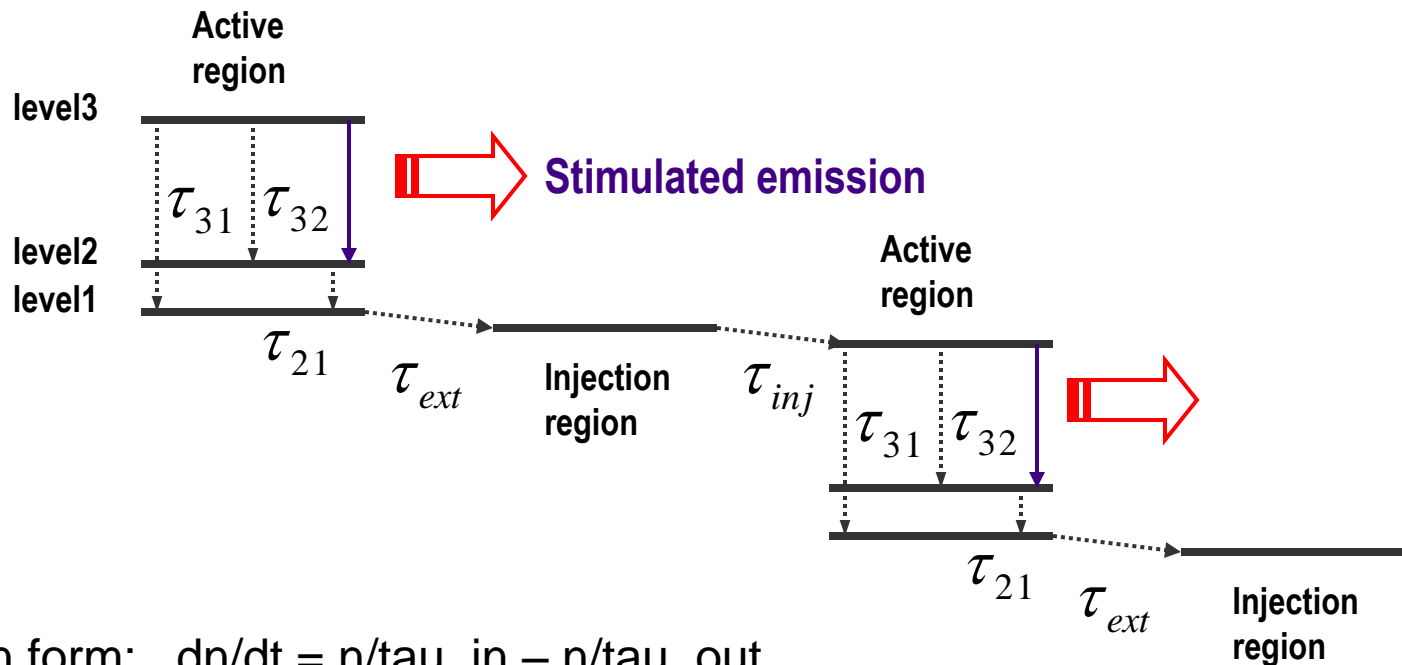




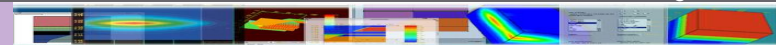
Following J. Kim et. al., IEEE JQE Vol. 40, p. 1663, 2004. Red lines: Conduction bands; Green lines: subband levels and envelop wave Functions. Blue line: macroscopic single Fermi level.



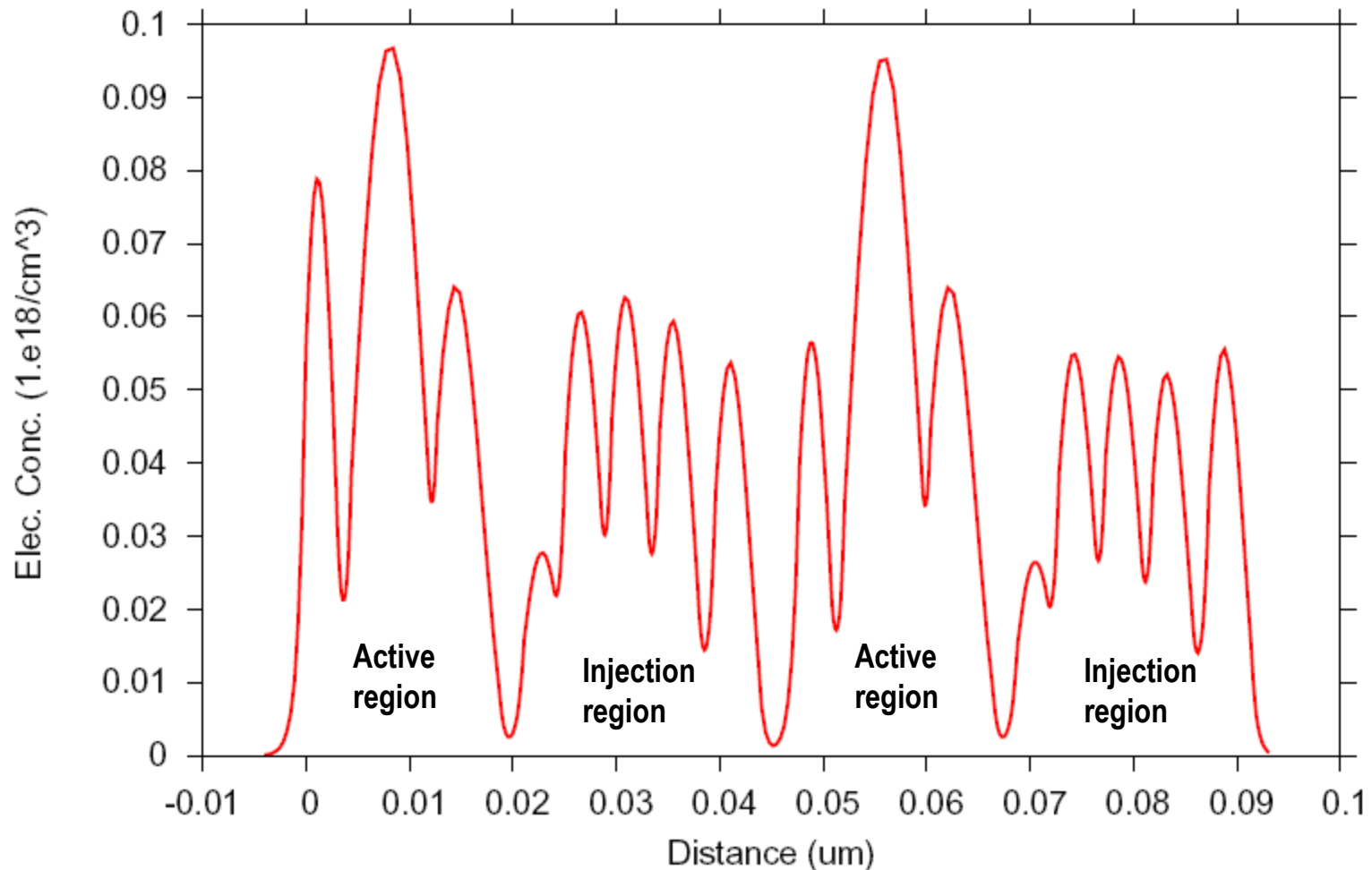
Microscopic rate equations



- Equations in form: $dn/dt = n/\tau_{in} - n/\tau_{out}$.
- Coupled with cavity photon rate equation.
- Relate device current to injection region current.
- Closed set of equations to get lasing characteristics.



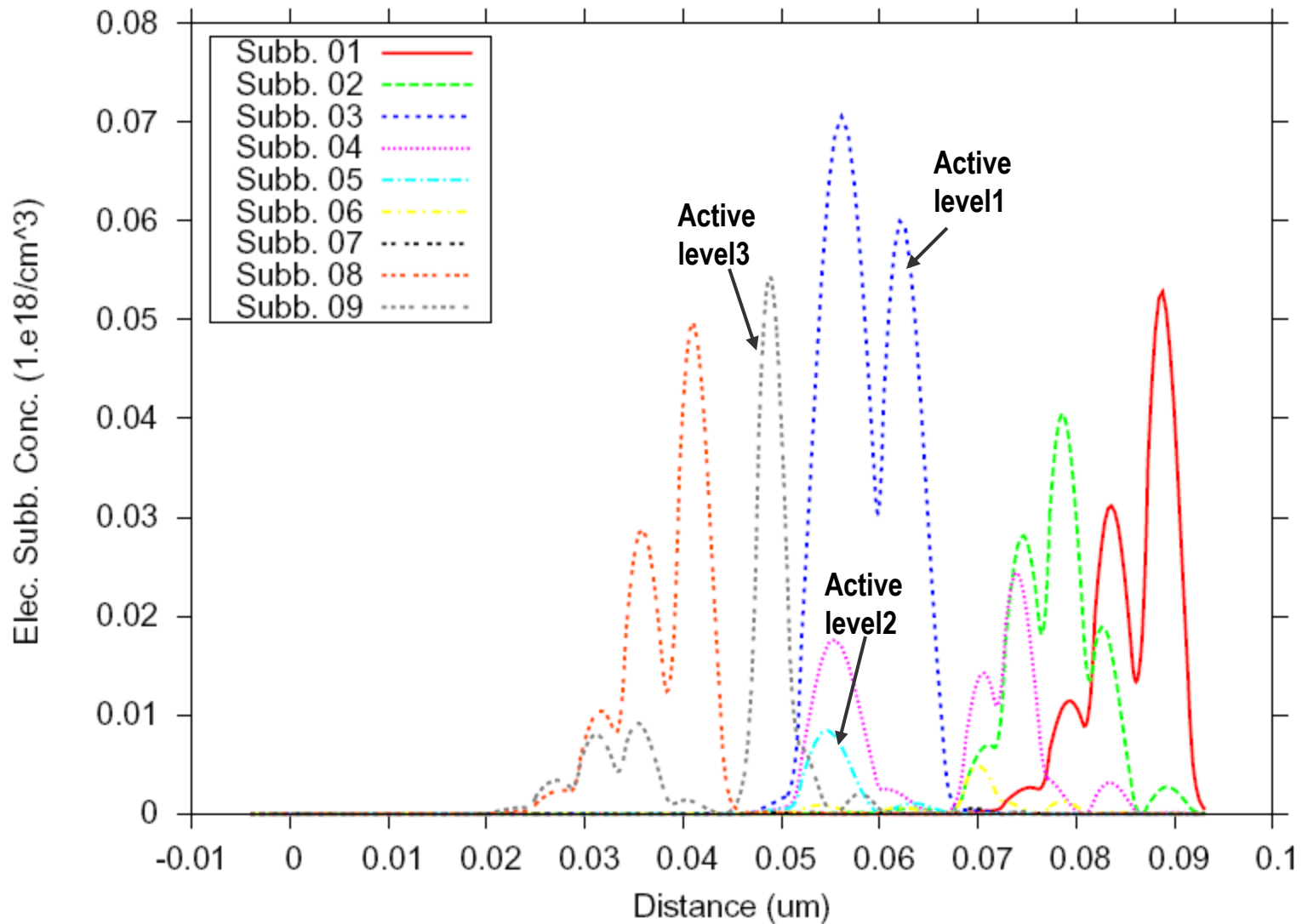
Distribution of Electrons



Electron distribution based on subband population
calculated by microscopic rate equations



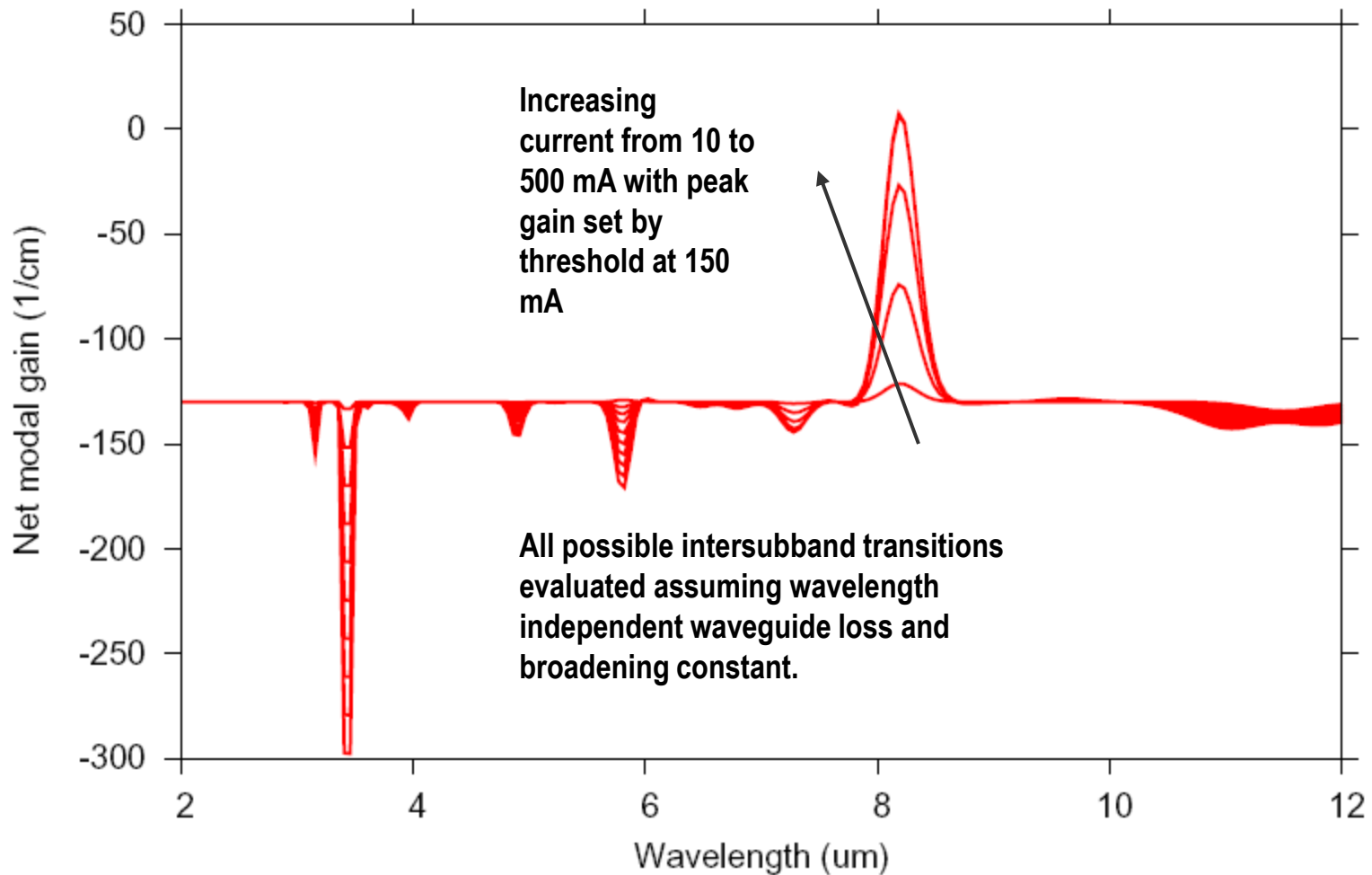
Distribution of subband electrons



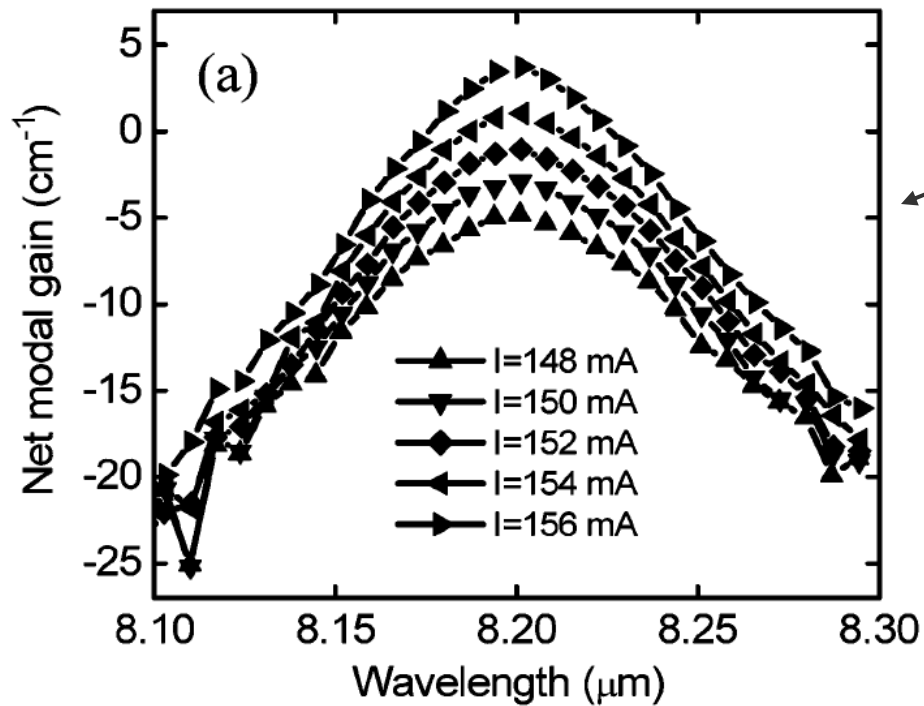
First 9 levels are plotted with the first three levels in active region labeled



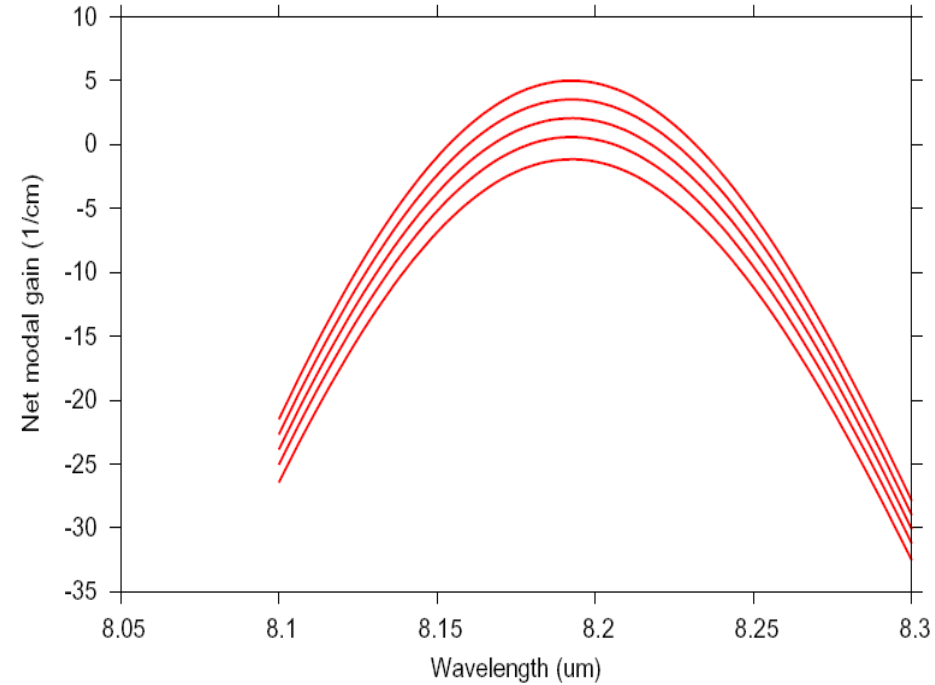
Gain spectrum-I



Gain spectrum-II



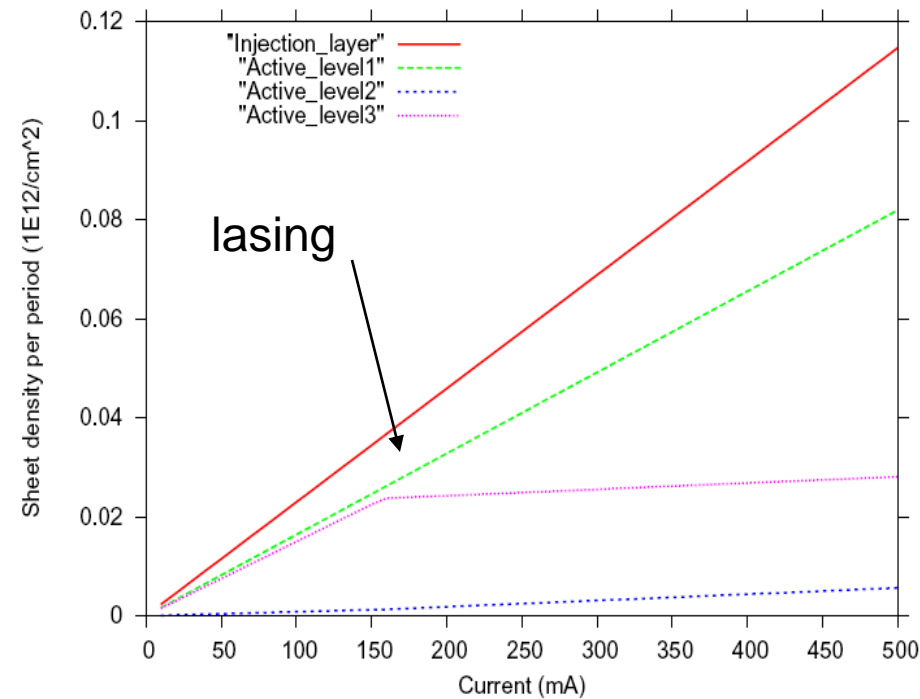
J. Kim et. al., IEEE JQE
Vol. 40, p. 1663, 2004



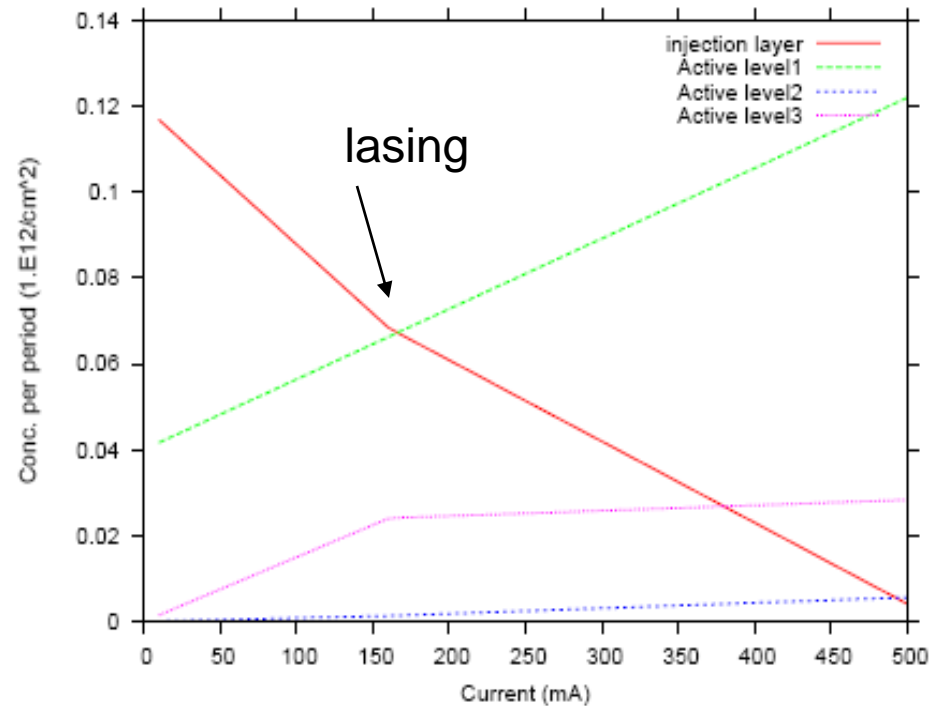
Reasonable agreement with experiment achieved.



Two injection schemes



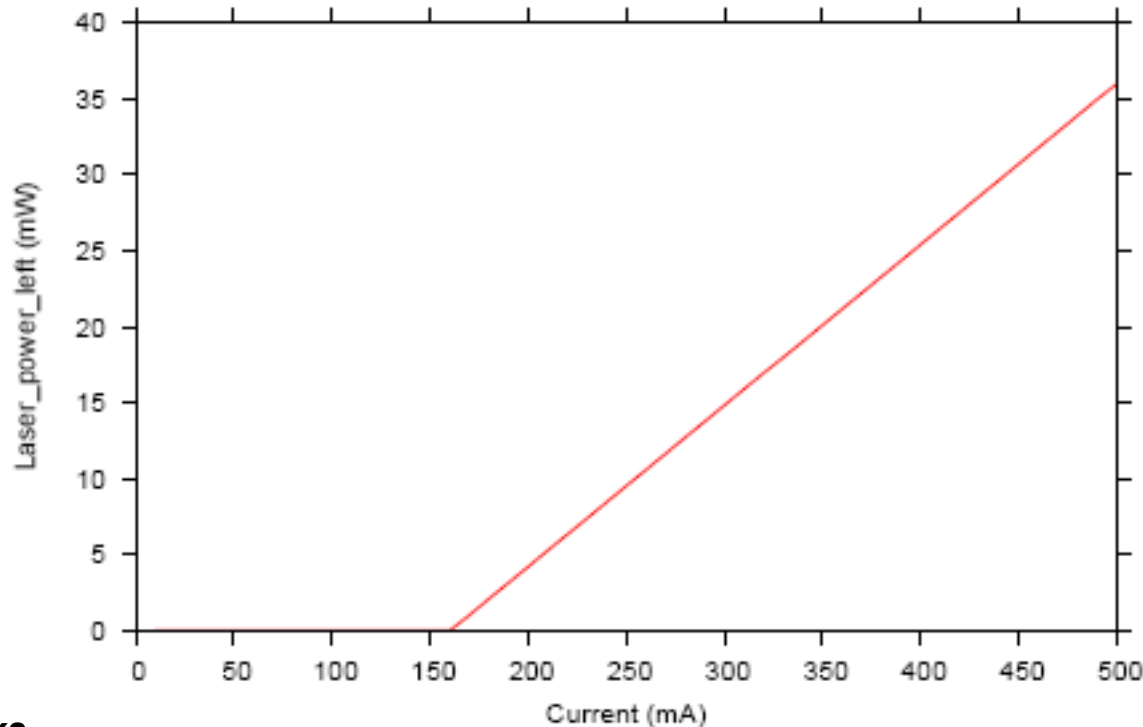
(a) Assume all τ 's are constants and all levels are initially unoccupied. Current injection increases occupancy until lasing.



(b) Assume injection region and active level1 are initially occupied. $1/\tau_{\text{injection}}$ set to increase linearly with current to preserve total sheet charge.

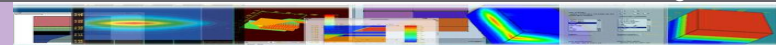


Both schemes result in same lasing characteristics



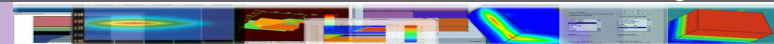
Remarks

- Stimulated recombination in QC laser does not pin the carrier density but only levels it off. Overall densities in active region still increase substantially as current is injected.
- Lack of density pinning explains absence of lasing relaxation oscillation in laser turn-on/off.
- Lasing action does not require or imply charge neutrality.

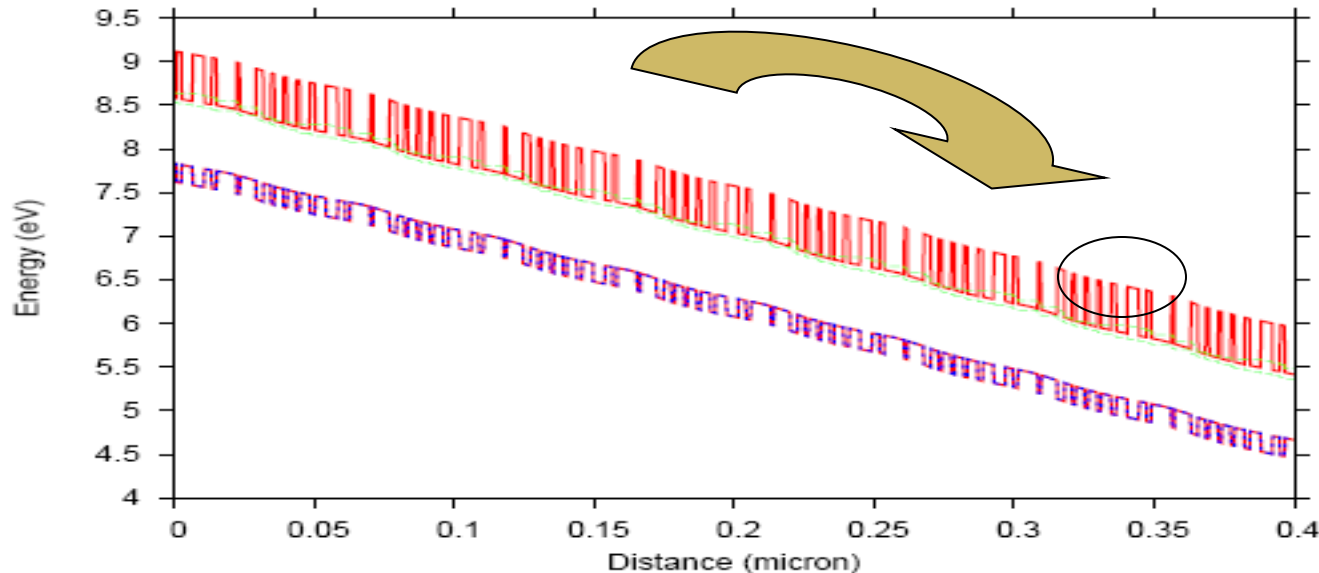


Contents

- ➡ Microscopic rate equation approach
- ➡ **Challenge in carrier transport modeling**
- ➡ Solution in 2/3D simulator



Challenges in transport modeling



■ Microscopic rate equations:

- Time constants contain no information on how electrons get there from the contacts.
- One still has to work on transport on larger size scale.

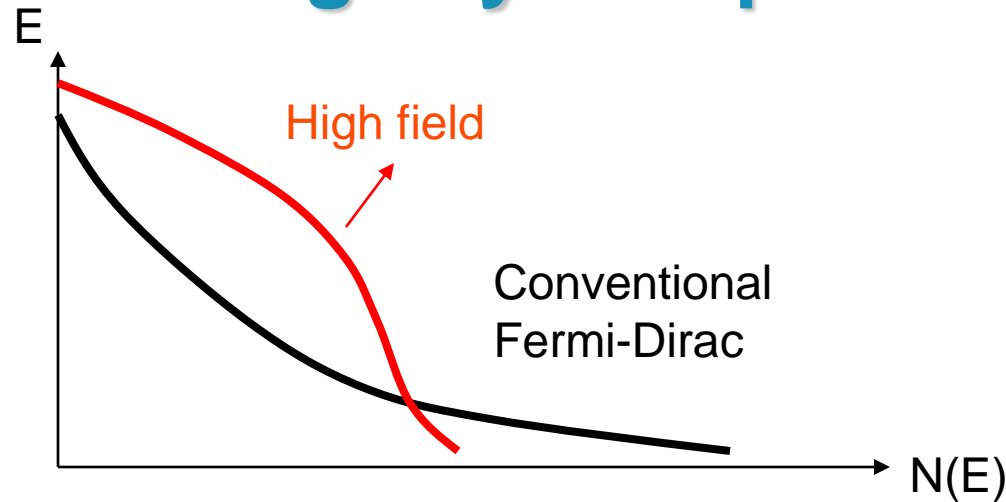


Challenges in transport modeling

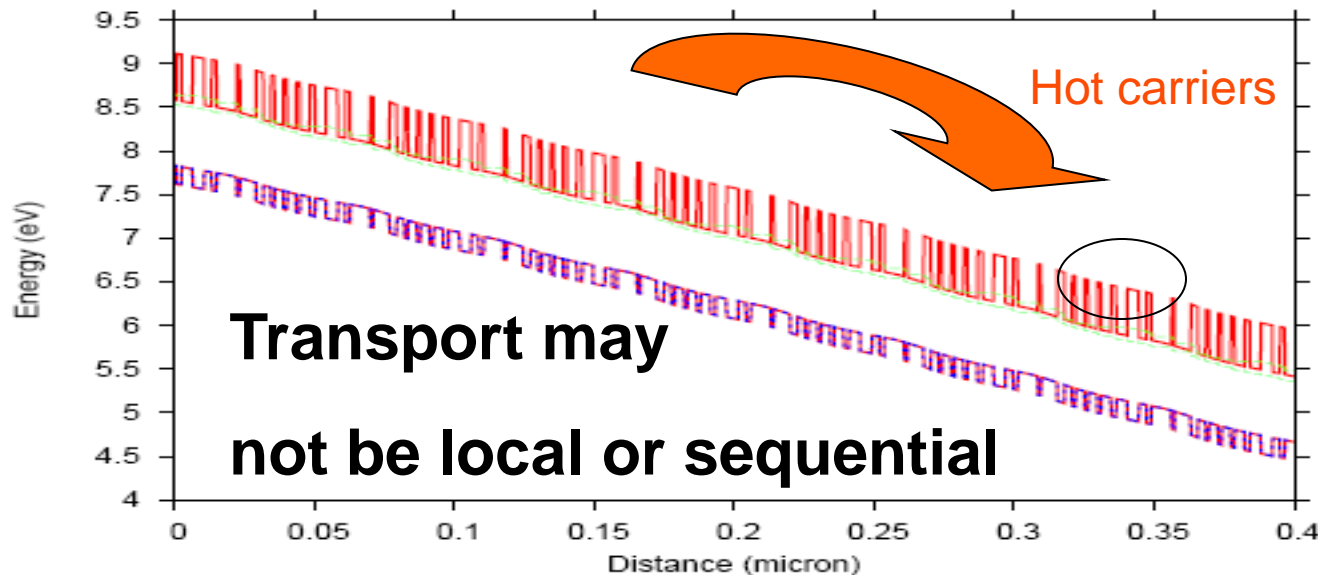
- **Commonly used device simulators:**
 - Mobility-based drift-diffusion and thermionic emission.
 - Quantum tunneling done for few barriers as correction to drift-diffusion model.
- **Requirement for QCL:**
 - Drift-diffusion and thermionic emission still needed.
 - Quantum tunneling for hundreds of barriers.



Going beyond quasi-equilibrium?



**Tunneling
emitter src**



Contents

- ➡ Microscopic rate equation approach
- ➡ Challenge in carrier transport modeling
- ➡ **Solution in 2/3D simulator**



Equations and models

■ The conventional:

- Drift-diffusion equations with thermionic boundary.
- Scalar optical mode solver.
- Laser cavity photon rate equation.

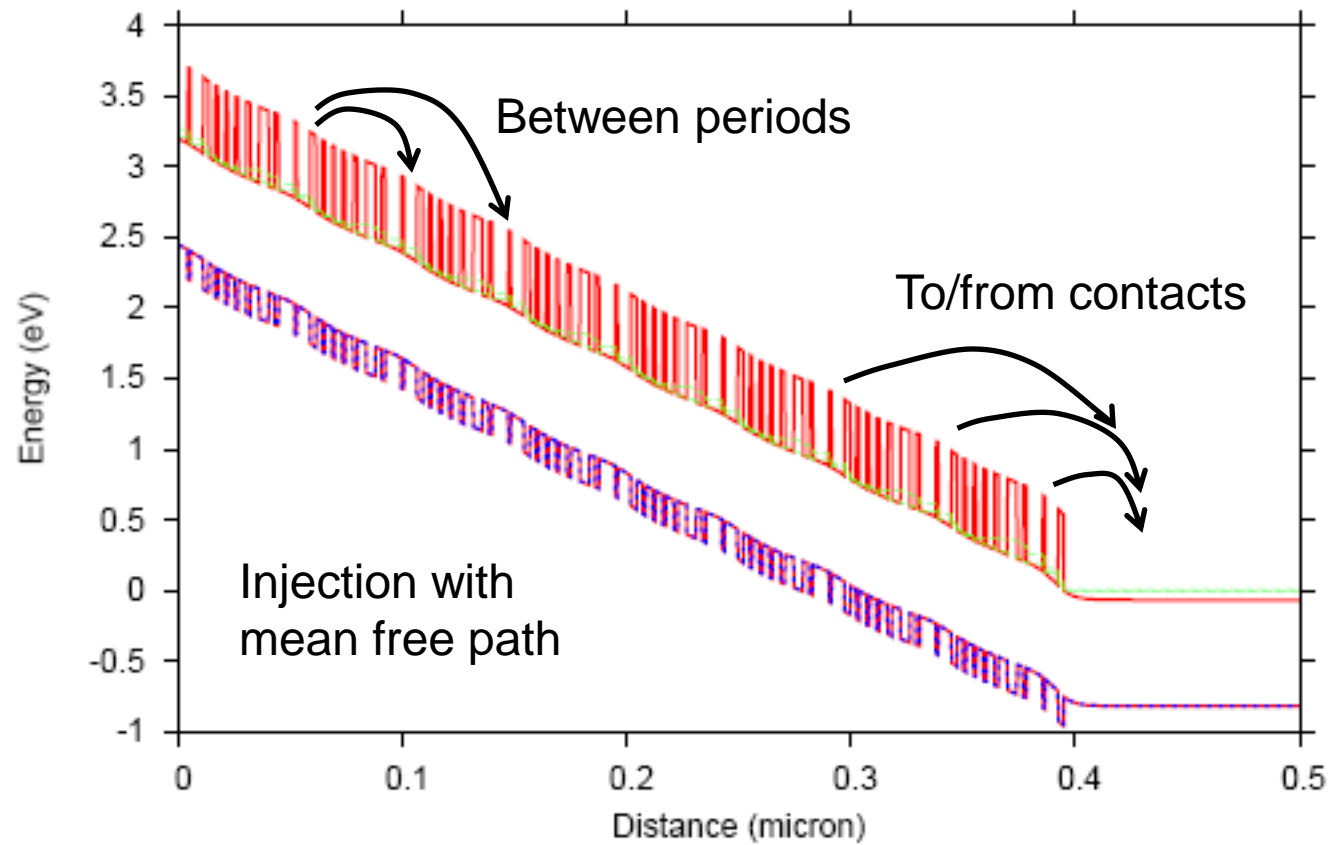
■ QCL specifics:

- Local optical gain as a function of local current according to microscopic rate: $g(J, S)$.
- Within period: transport between injection/active regions according to microscopic rate eq.
- Non-local transport between periods and to/from contacts.

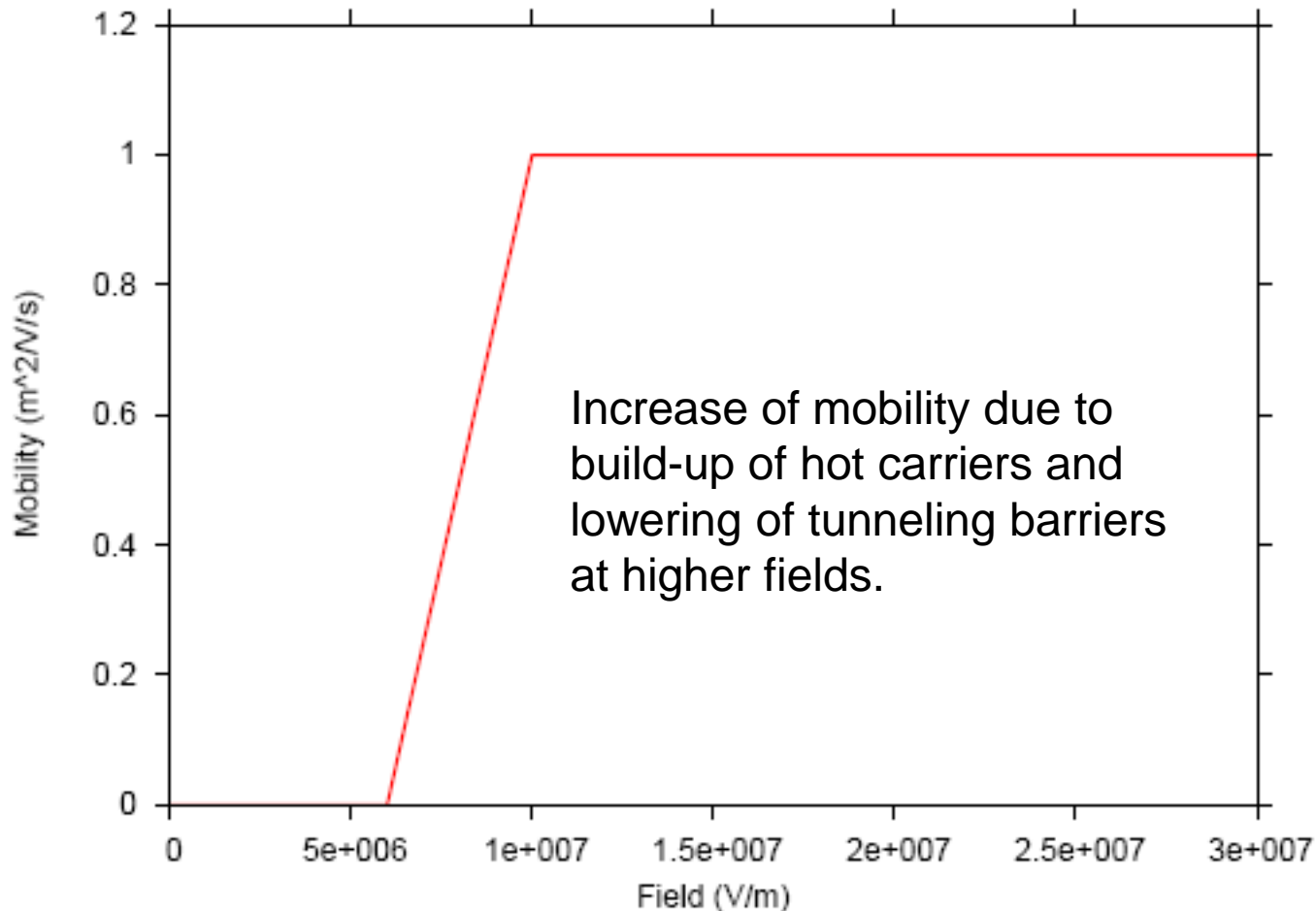
Resonant
tunneling
effects



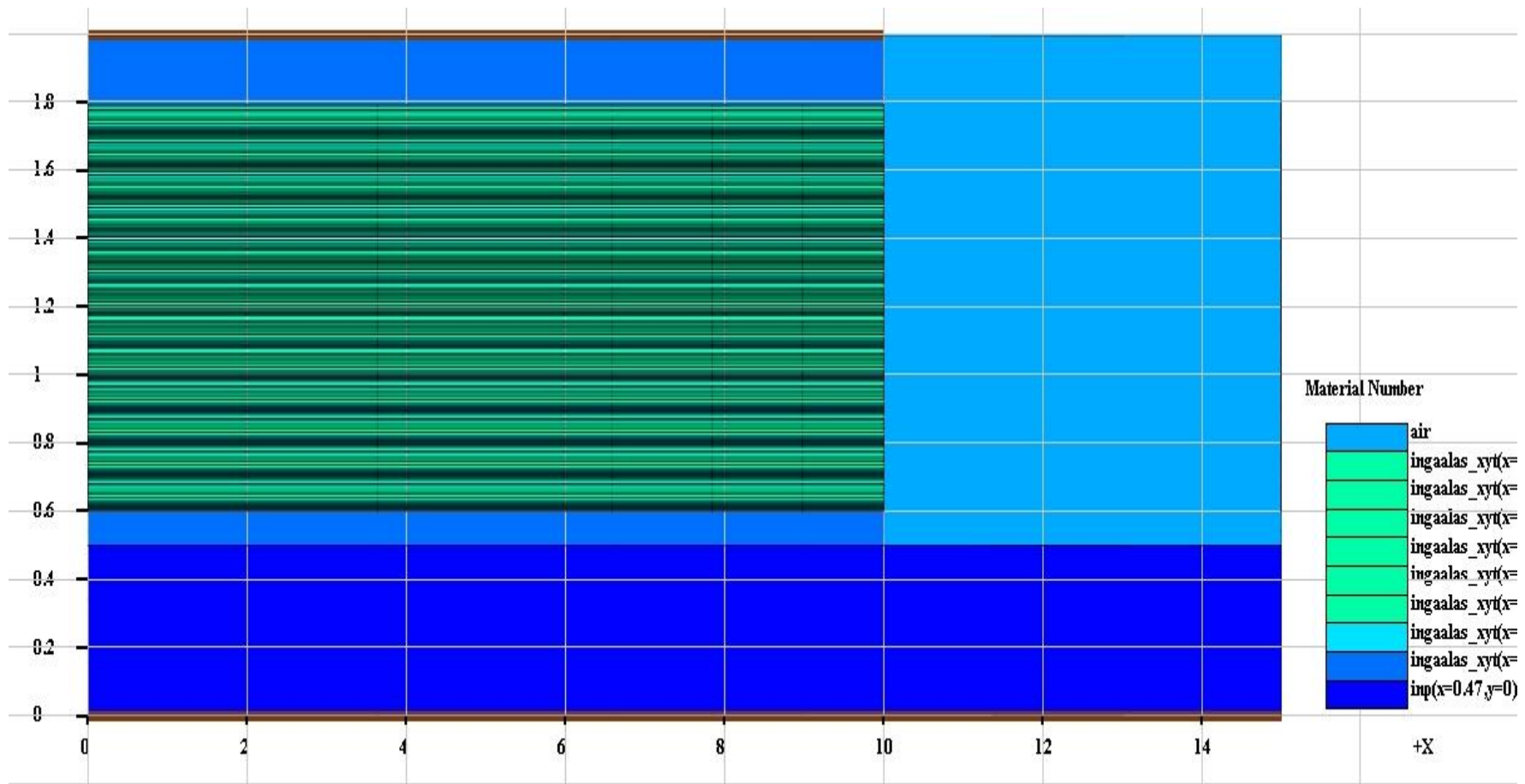
Non-local injection model



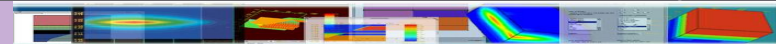
Non-local injection mobility



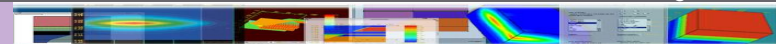
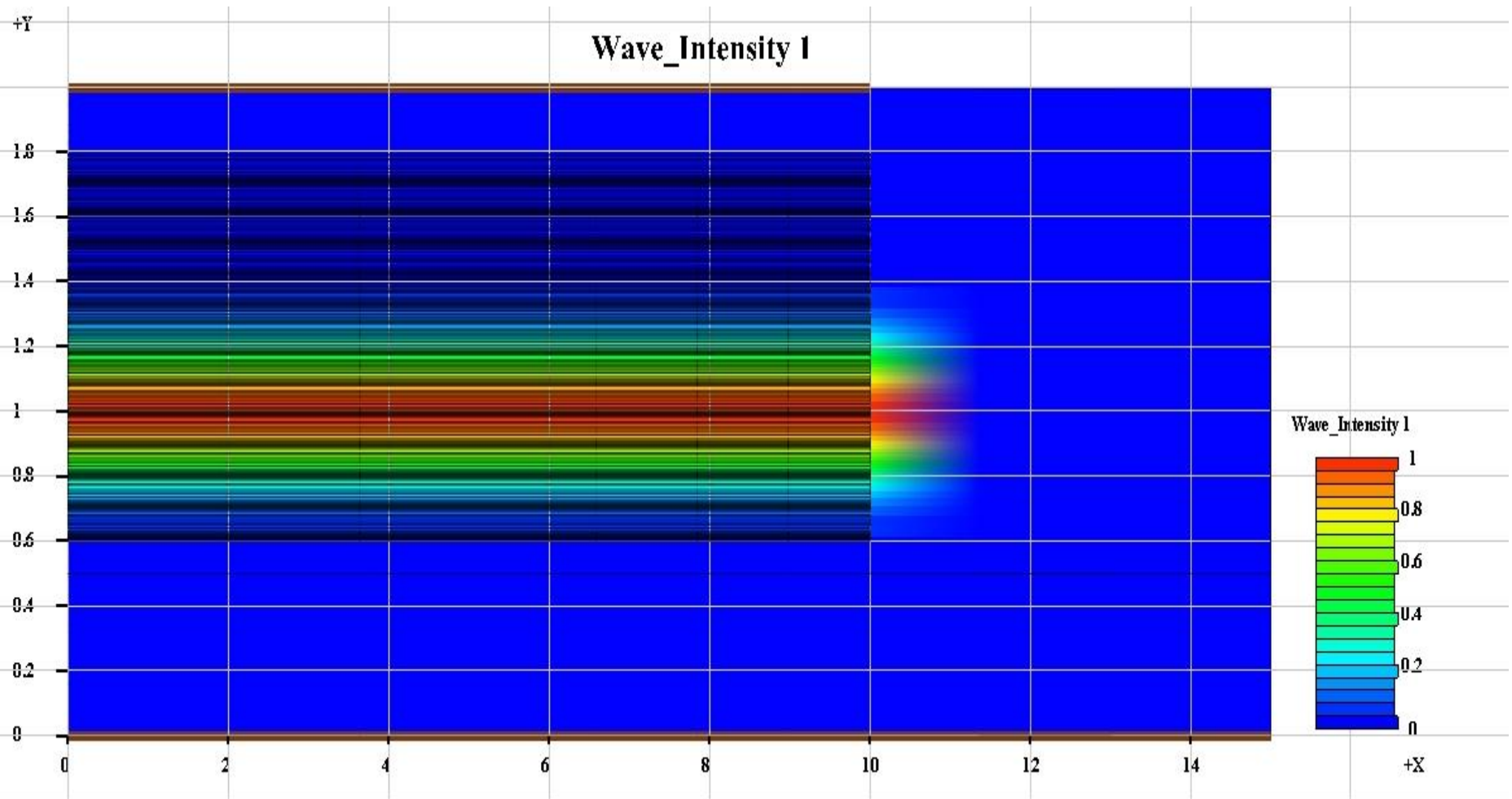
QCL 2D example



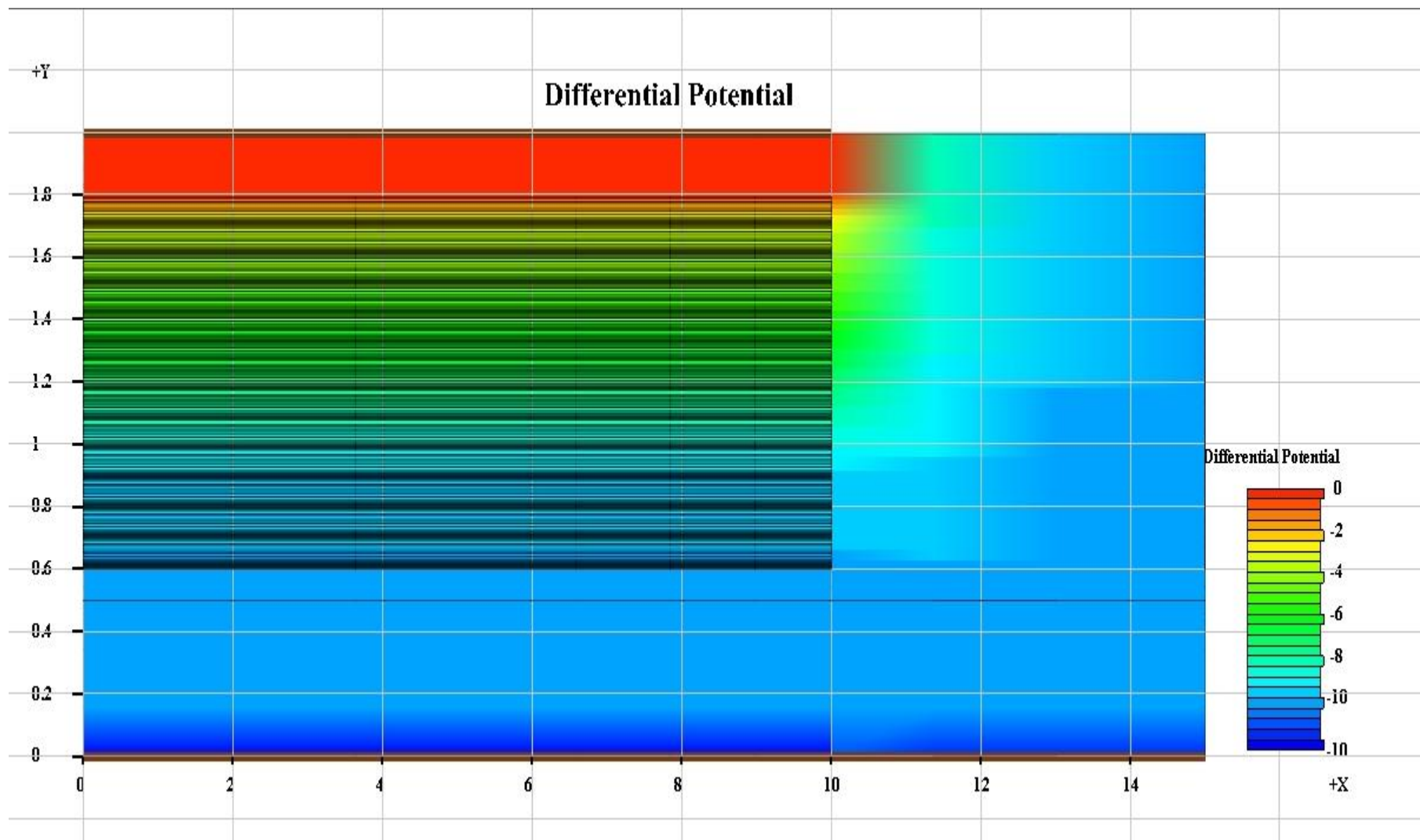
25 periods, assuming same MQW and microscopic rates as in previous sections.



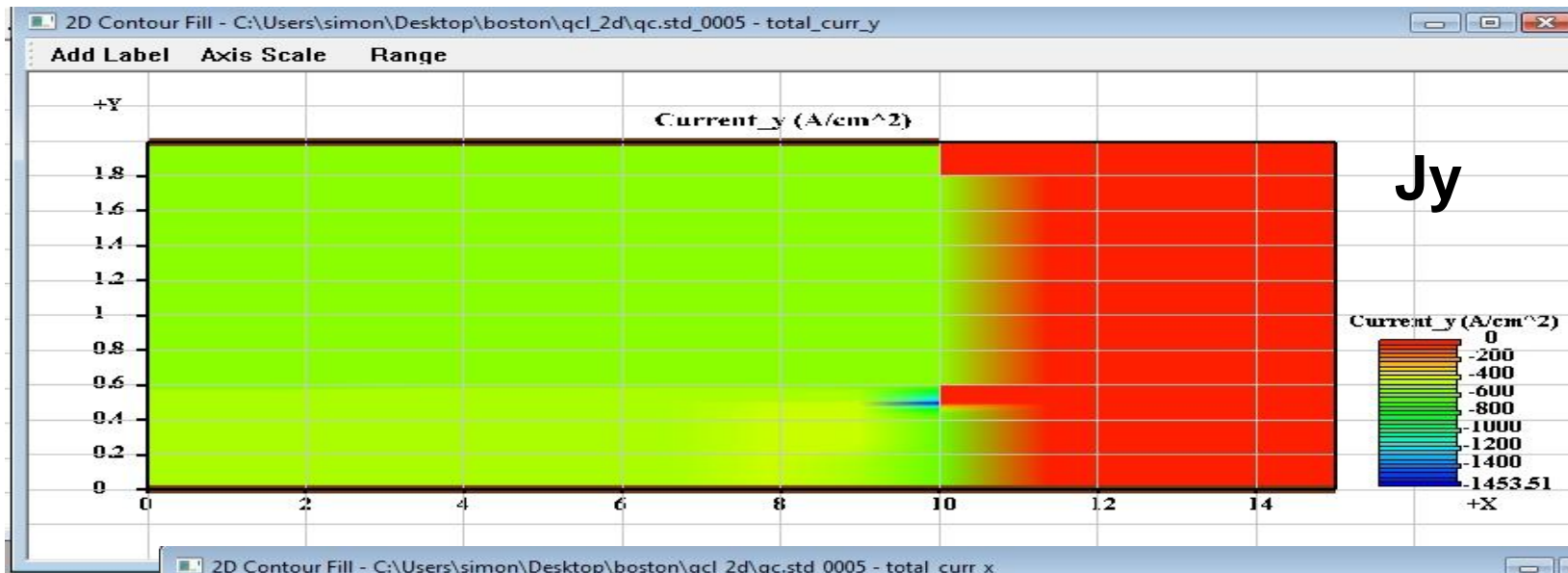
Optical mode



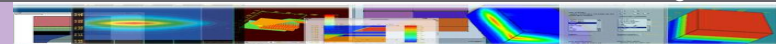
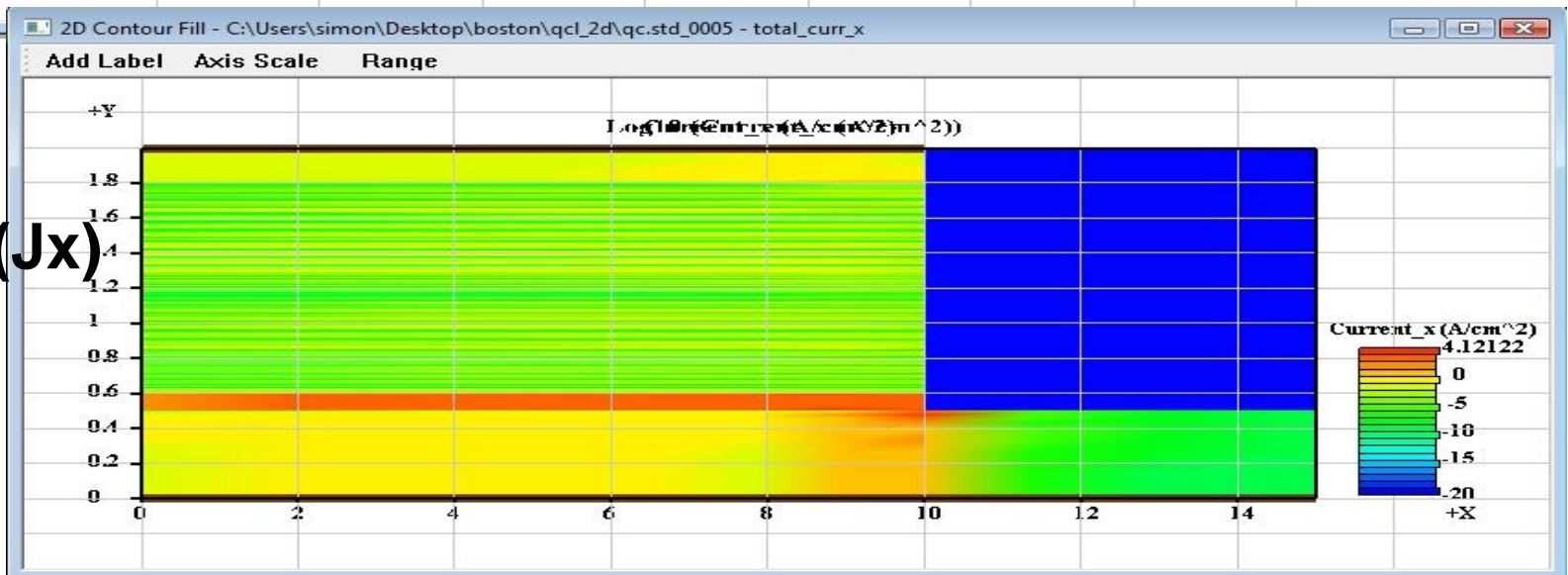
Applied potential



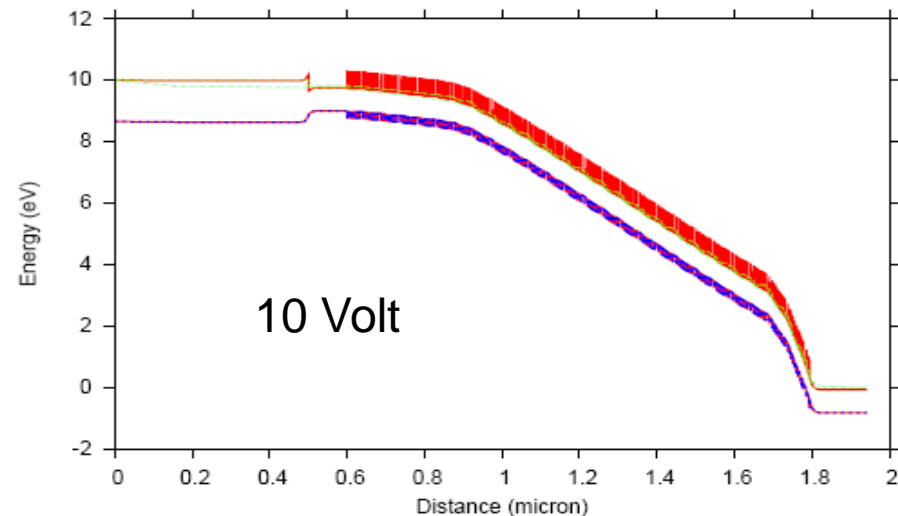
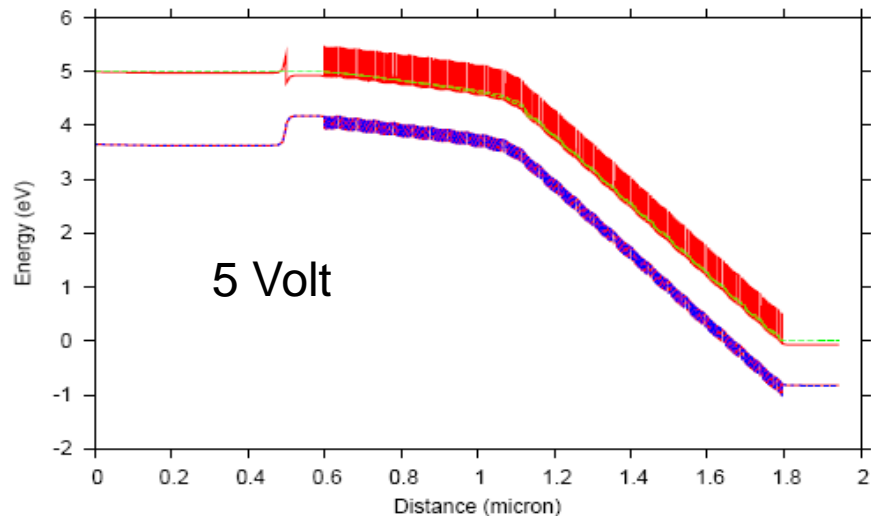
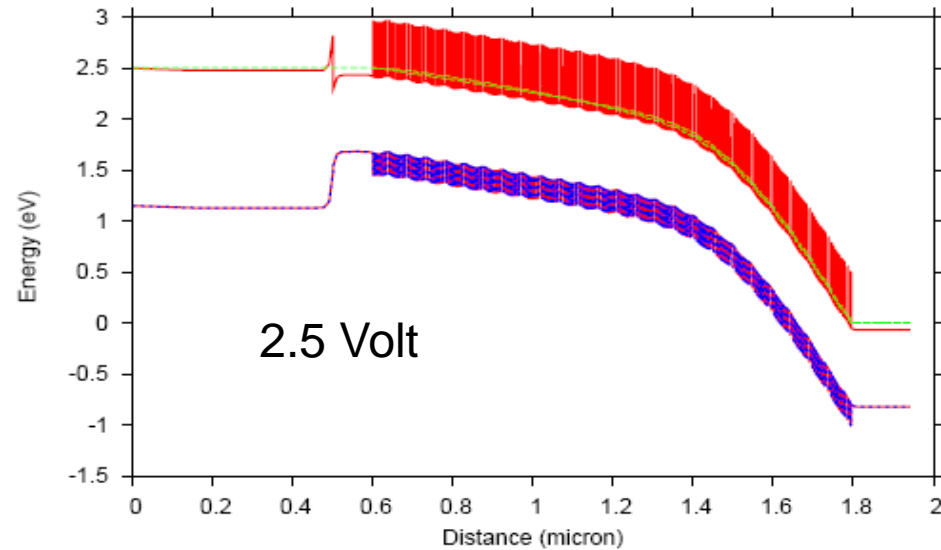
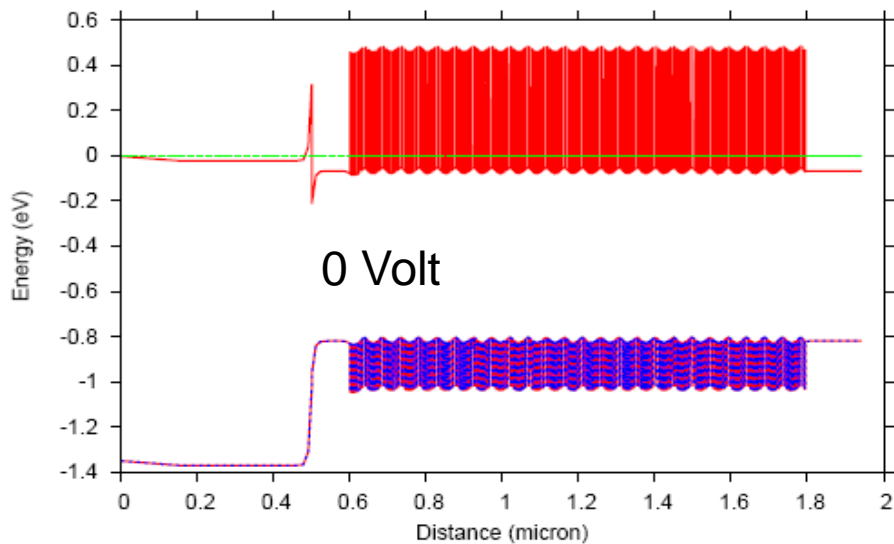
Current distribution



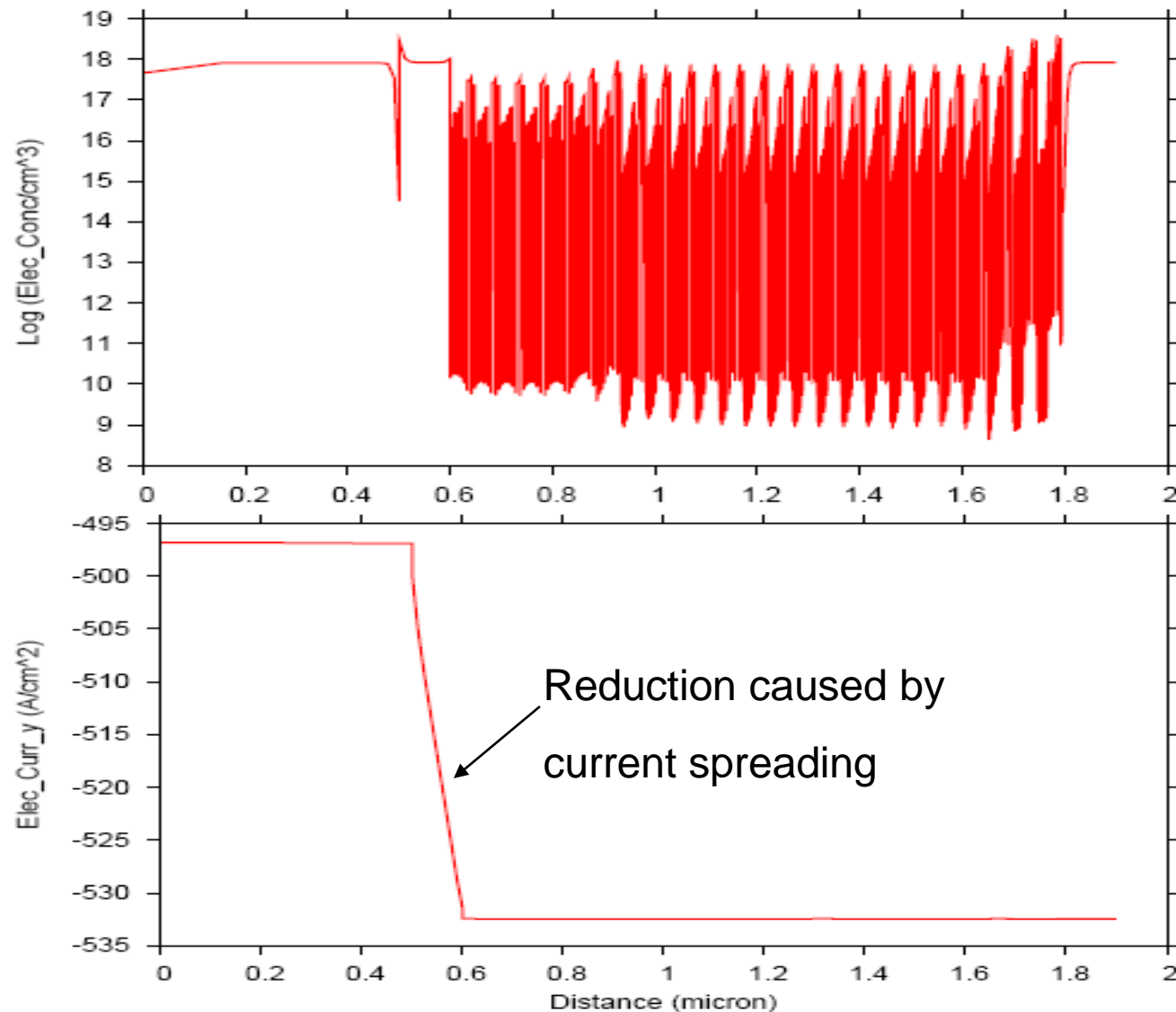
Log10(Jx)



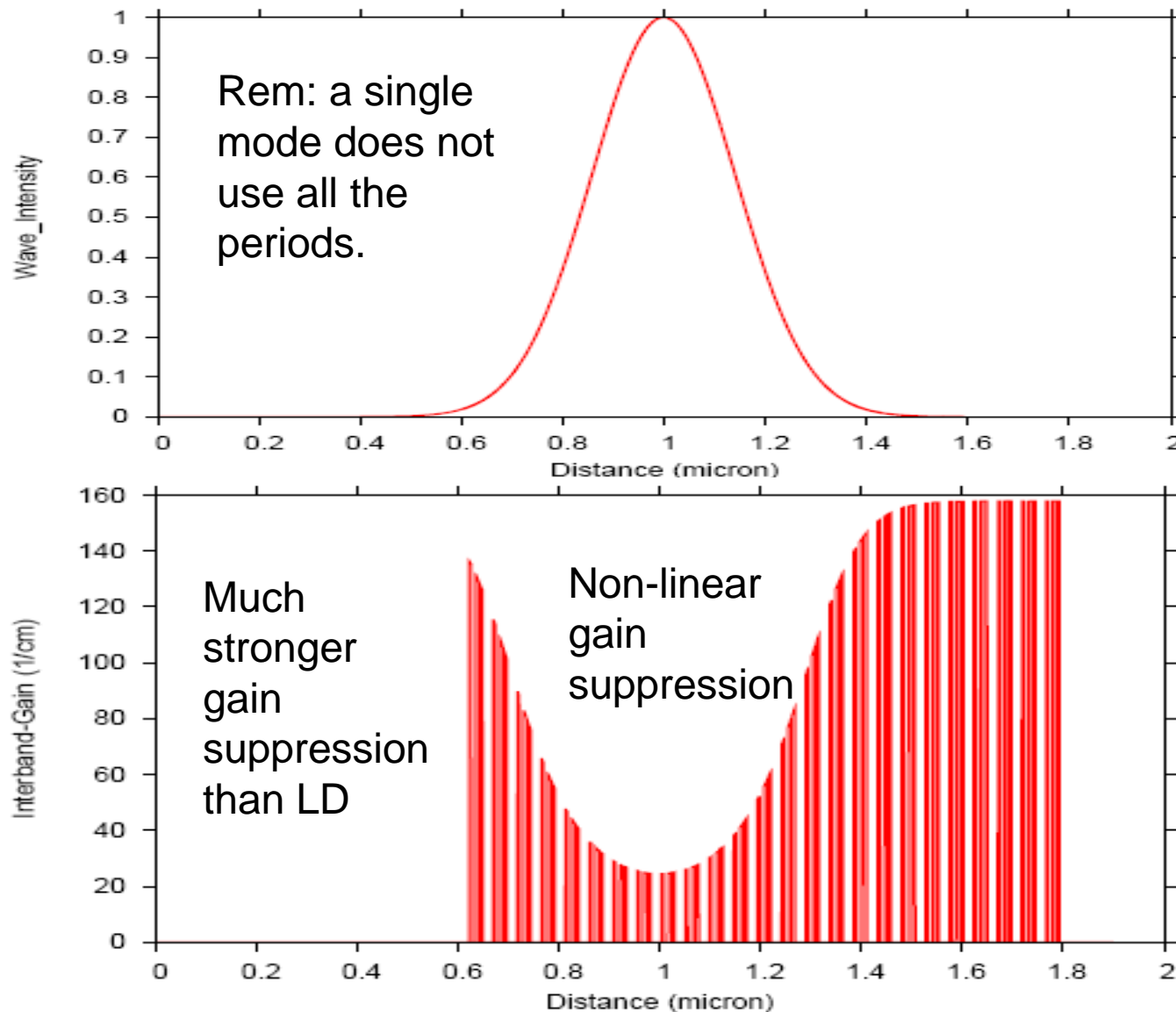
Band diagrams (QCL 25 periods)



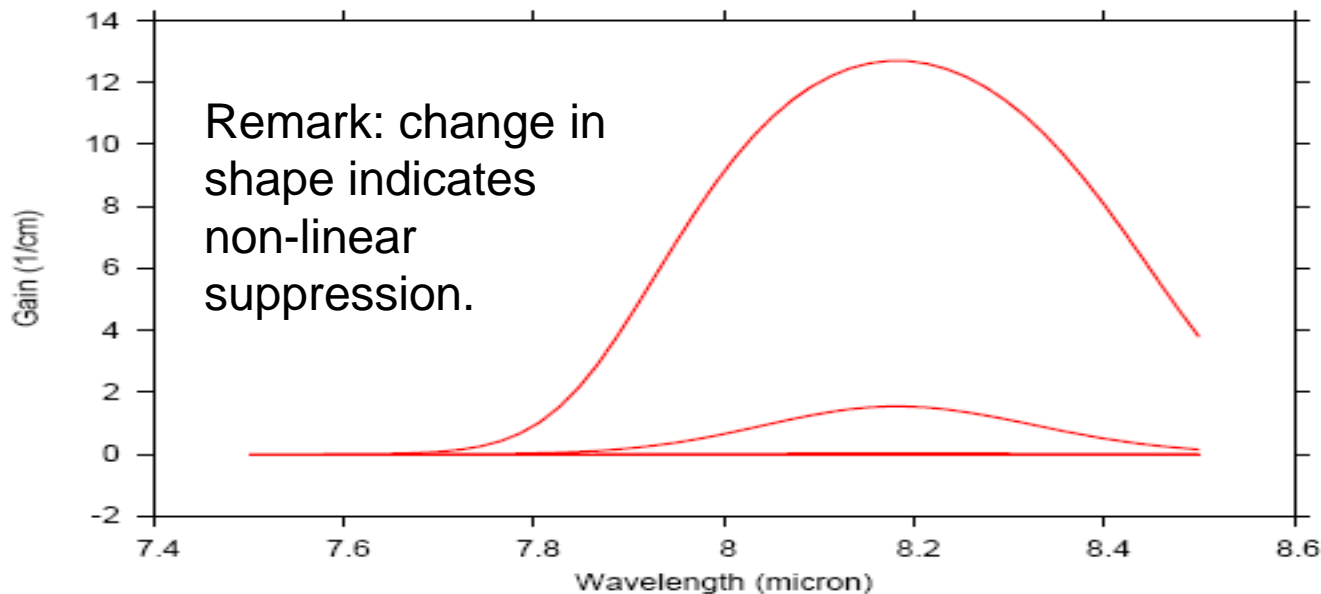
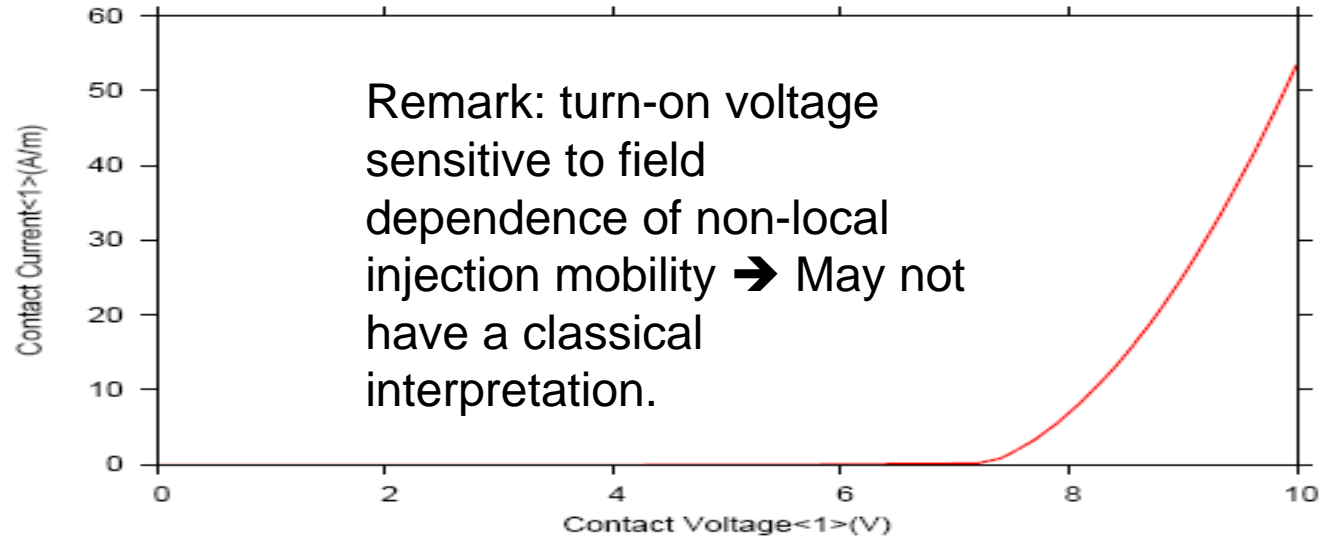
1D cuts of electron concentration and J_y (@10 V)



1D cuts of optical intensity and optical gain (@10 V)



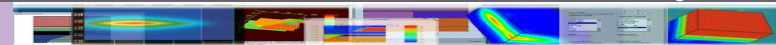
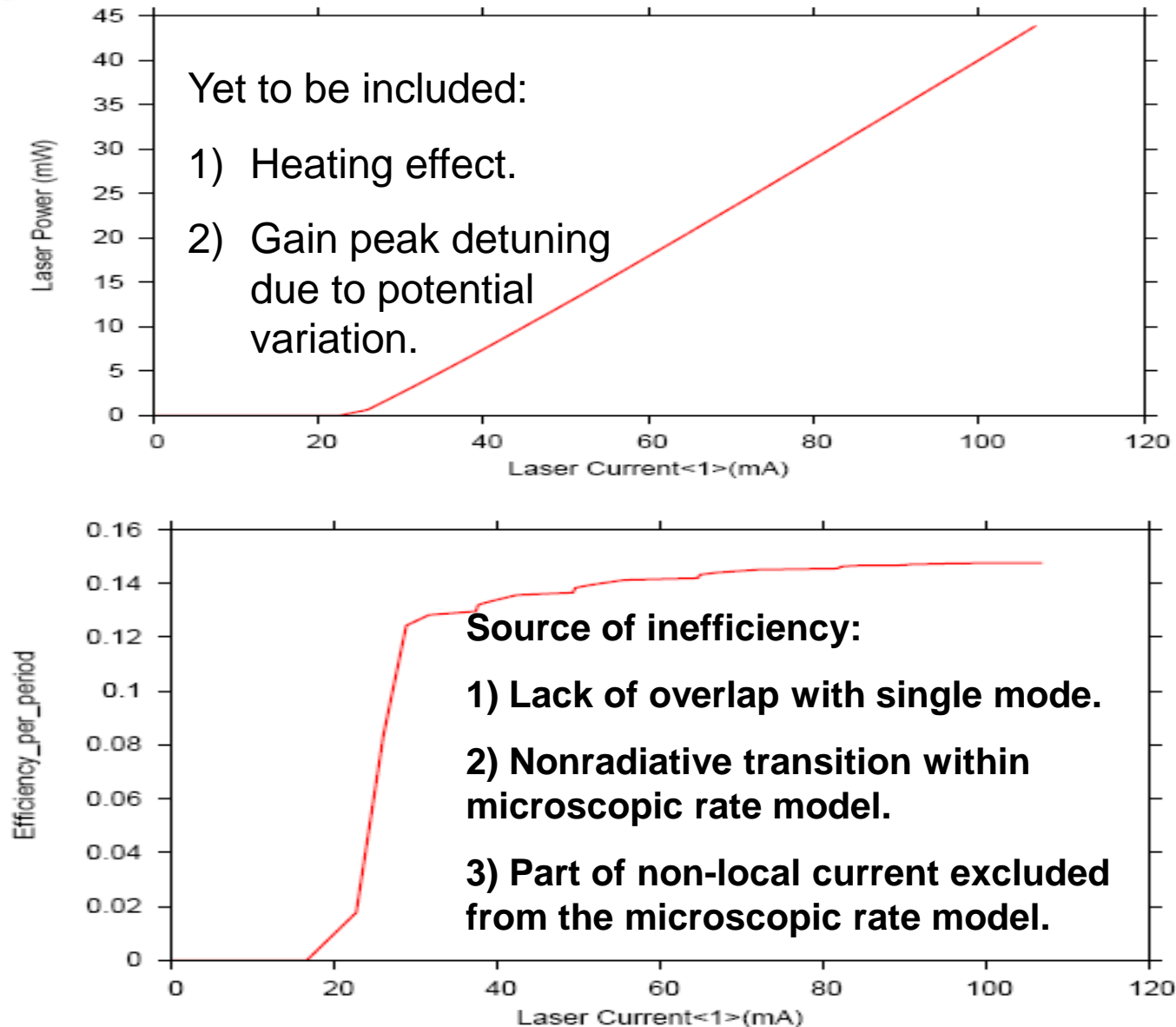
I-V and modal gain spectrum



Modal gain at 0, 2.5, 5, 7.5 and 10 volts.

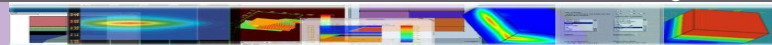


Lasing characteristics and efficiency per period



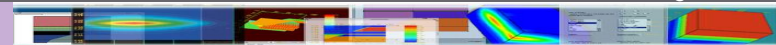
Summary

- Subband structure calculation enables the basic design of QCL such as emission wavelength and miniband alignments.
- Microscopic rate equation model generates a convenient optical gain as a function of local current and photon densities $g(J,S)$.
- Main challenge in macroscopic QCL simulation is to inject electrons from contact to MQW and to collect them from MQW to contact.
- We propose a non-local current injection model with a mean-free-path of 100 -1000 Å.
- Field dependent mobility of non-local injection needed to obtain reasonable results.



About Crosslight

- A leading semiconductor TCAD provider since 1993
- Complete product portfolio for semiconductor device simulation
- Innovative simulation tools to ensure a fast and seamlessly transfer from process to device simulation
- Ultra efficient 3D structure combined with powerful and easy to use 3D editor to provide class leading 3D simulation experience
- “Café-time Simulator”. Windows based, user friendly graphic user interface makes simulation more enjoyable.



Creators of Award Winning Software

CROSSLIGHT Software Inc.

